

$$\exp x \underset{x \rightarrow 0}{=} \sum_{k=0}^n \frac{x^k}{k!} + o(x^n)$$

$$\exp x \underset{x \rightarrow 0}{=} 1 + x + \frac{x^2}{2} + \frac{x^3}{6} + \dots + \frac{x^n}{n!} + o(x^n)$$

$$\operatorname{ch} x \underset{x \rightarrow 0}{=} \sum_{k=0}^n \frac{x^{2k}}{(2k)!} + o(x^{2n+1})$$

$$\operatorname{ch} x \underset{x \rightarrow 0}{=} 1 + \frac{x^2}{2} + \frac{x^4}{24} + \dots + \frac{x^{2n}}{(2n)!} + o(x^{2n+1})$$

$$\operatorname{sh} x \underset{x \rightarrow 0}{=} \sum_{k=0}^n \frac{x^{2k+1}}{(2k+1)!} + o(x^{2n+2})$$

$$\operatorname{sh} x \underset{x \rightarrow 0}{=} x + \frac{x^3}{6} + \frac{x^5}{120} + \dots + \frac{x^{2n+1}}{(2n+1)!} + o(x^{2n+2})$$

$$\cos x \underset{x \rightarrow 0}{=} \sum_{k=0}^n (-1)^k \frac{x^{2k}}{(2k)!} + o(x^{2n+1})$$

$$\cos x \underset{x \rightarrow 0}{=} 1 - \frac{x^2}{2} + \frac{x^4}{24} + \dots + (-1)^n \frac{x^{2n}}{(2n)!} + o(x^{2n+1})$$

$$\sin x \underset{x \rightarrow 0}{=} \sum_{k=0}^n (-1)^k \frac{x^{2k+1}}{(2k+1)!} + o(x^{2n+2})$$

$$\sin x \underset{x \rightarrow 0}{=} x - \frac{x^3}{6} + \frac{x^5}{120} + \dots + (-1)^n \frac{x^{2n+1}}{(2n+1)!} + o(x^{2n+2})$$

$$\tan(x) \underset{x \rightarrow 0}{=} x + \frac{x^3}{3} + o(x^3)$$

$$\frac{1}{1-x} \underset{x \rightarrow 0}{=} \sum_{k=0}^n x^k + o(x^n)$$

$$\frac{1}{1-x} \underset{x \rightarrow 0}{=} 1 + x + x^2 + x^3 + \dots + x^n + o(x^n)$$

$$\frac{1}{1+x} \underset{x \rightarrow 0}{=} \sum_{k=0}^n (-1)^k x^k + o(x^n)$$

$$\frac{1}{1+x} \underset{x \rightarrow 0}{=} 1 - x + x^2 - x^3 + \dots + (-1)^n x^n + o(x^n)$$

$$\ln(1+x) \underset{x \rightarrow 0}{=} \sum_{k=1}^n (-1)^{k-1} \frac{x^k}{k} + o(x^n)$$

$$\ln(1+x) \underset{x \rightarrow 0}{=} x - \frac{x^2}{2} + \frac{x^3}{3} + \dots + (-1)^{n+1} \frac{x^n}{n} + o(x^n)$$

$$\operatorname{Arctan} x \underset{x \rightarrow 0}{=} \sum_{k=0}^n (-1)^k \frac{x^{2k+1}}{2k+1} + o(x^{2n+2})$$

$$\operatorname{Arctan} x \underset{x \rightarrow 0}{=} x - \frac{x^3}{3} + \dots + (-1)^n \frac{x^{2n+1}}{2n+1} + o(x^{2n+2})$$

$$(1+x)^\alpha \underset{x \rightarrow 0}{=} \sum_{k=0}^n \frac{\alpha(\alpha-1)\dots(\alpha-k+1)}{k!} x^k + o(x^n)$$

pour  $n = 2$  :

$$(1+x)^\alpha \underset{x \rightarrow 0}{=} 1 + \alpha x + \frac{\alpha(\alpha-1)}{2} x^2 + o(x^2)$$

pour  $\alpha = \frac{1}{2}$  et  $n = 3$  :

$$\sqrt{1+x} \underset{x \rightarrow 0}{=} 1 + \frac{1}{2}x - \frac{1}{8}x^2 + \frac{1}{16}x^3 + o(x^3)$$

$$\sqrt{1-x} \underset{x \rightarrow 0}{=} 1 - \frac{1}{2}x - \frac{1}{8}x^2 - \frac{1}{16}x^3 + o(x^3)$$